# Supplementary Material: Neural Shift-Reduce CCG Semantic Parsing

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## 1 Number of Operations in Shift-Reduce and CKY CCG Parsers

Let  $\Lambda$  be a CCG lexicon,  $\mathcal{R}_b$  the set of binary CCG rules, and  $\mathcal{R}_u$  the set of unary CCG rules. While in practice lexical entries may map phrases to categories, for simplification, we assume that each lexical entry contains only one token.<sup>1</sup> Let  $|\lambda|$  be the number of lexical entries for a token in  $\Lambda$ . We assume an input sentence x with m tokens. We define an operation in shift-reduce parsing to be the application of a single action to a configuration. In CKY, an operation is an application of a unary rule to a cell in the chart, or a binary rule to a pair of adjacent cells.

**CKY CCG Semantic Parser** CKY parsing starts with populating the chart using the lexicon  $\Lambda$ . Under our single-token assumption, this requires at most  $m|\lambda|$  operations. In practice, though, the number of categories maintained in each cell is capped by a beam of size k. We denote a cell that spans the token sequence  $\langle x_i, \ldots, x_j \rangle$  as [i, j]. Given the cell [i, j], j > i, CKY considers all possible splits  $\{\langle [i,l], [l+1,j] \rangle \mid i \leq l \leq j\}$  of this cell and applies binary rules  $b \in \mathcal{R}_b$  to the categories in the cells [i, l] and [l+1, j]. This requires  $mk^2 |\mathcal{R}_b|$  operations due to O(m) possible splits,  $k^2$  possible categories from the beams of the two cells, and  $|\mathcal{R}_h|$ binary rules. There is a total of  $m^2$  cells. Therefore, the total number of operations for binary rules is  $m^3k^2|\mathcal{R}_b|$ . For every cell, we can also apply a unary rule from  $\mathcal{R}_{u}$ . The overall number of unary operations is  $m^2 k |\mathcal{R}_u|$ . The total number of operations is  $O(m|\lambda| + m^3k^2|\mathcal{R}_b| + m^2k|\mathcal{R}_u|).$ 

Shift-Reduce CCG Semantic Parser The shiftreduce parser also uses a beam of size k. The beam maintains the k max-scoring configurations. At each step, it applies all possible actions to each configuration in the beam to generate a new configuration. The top-k new configurations are then retained in the beam. We can perform shift for each token on the buffer, which give m operations. Since binary reduce removes an element from the stack, we can do at most m-1 such operations. We disallow two consecutive unary reduce actions. Therefore, unary reduce actions must follow a shift or a binary reduce, which translates to at most m - 1 + m = 2m - 1operations. Therefore, the parser necessarily terminates after at most 4m - 2 beam expansions. For a given configuration, we can apply  $|\lambda| + |\mathcal{R}_b| + |\mathcal{R}_u|$ actions. In every step of the algorithm there are at most k configurations to process, giving a total of  $O(4mk(|\lambda| + |\mathcal{R}_b| + |\mathcal{R}_u|))$  operations

Quantitative Comparison In our experiments, the lexicon  $\Lambda$  contains 1.7M entries for 11K words and phrases. If we define  $|\lambda|$  to be the mean number of entries, we get  $|\lambda| = 170$ . The average sentence length m in the data is 25. Our CCG has 30 binary rules ( $\mathcal{R}_b$ ) and 24 unary rules ( $\mathcal{R}_u$ ). Artzi et al. (2015) use a beam size of 50 in their CKY parser, which gives roughly 10<sup>9</sup> operations per sentence of length 25. For our final results, we use a beam of 512, which gives roughly 10<sup>7</sup> operations for the same length, two orders of magnitude fewer.

<sup>&</sup>lt;sup>1</sup>Generalization to multiple tokens is straightforward.

Feature Type	Dimension	Description
RULE-NAME	16	Action name
POS	12	POS tags of all tokens removed from the buffer in a SHIFT operation
TEMPLATE∧RPOS	32	Template and POS tag of the first token on the buffer following a SHIFT (not
		triggered for reduce operations)
TEMPLATE∧LPOS	32	Template and POS tag of the last token consumed before a SHIFT (not triggered
		for reduce operations)
NEXT-POS1	12	POS of the first token on the buffer after an action
NEXT-POS2	12	POS of the second token on the buffer after an action
PREV-POS1	12	POS of the recently consumed token before an action
PREV-POS2	12	POS of the second recently consumed token before an action
Features from Artzi et al. (2015)		
LEX-TEMPLATE	48	Triggers four features on SHIFT operations:
		Lexeme of the lexical entry
		Template of the lexical entry
		Conjunction of lexeme and template
		Conjunction of template and POS of the lexical entry tokens
TypeShiftSem	32	Conjunction of a CCG type-shifting unary rule and the head predicate of the
		logical form
Attribute∧POS	32	Conjunction of attributes used in the lexical entry and token POS tags
DYN	8	Using a lexical entry dynamically generated (e.g., NER)
DYNSKIP	8	Skipping a word
LogExp	8	Repeating conjuncts in the root logical form
SLOPPYLEX	16	Using a lexical entry dynamically created with sloppy heuristics
TypeShift	16	Using a unary type-shifting rule
CROSS	16	Using a crossing composition binary rule
ATTACH	32	Entity-relation-entity logical form attachment features

Table 1: Sparse features used for action embedding

## 2 Action Features

Table 1 lists the features used to compute action embeddings  $\phi(a, c)$ . Each feature is mapped to its embedding representation via a lookup table. The embeddings are then concatenated to create the action representation. We use a factored lexicon representation (Kwiatkowski et al., 2011), where entries are dynamically generated by combining lexemes and templates. For example, the lexical entry: remain  $\vdash S \setminus NP_{[pl]}/(N_{[pl]}/N_{[pl]})$ :  $\lambda f.\lambda x.f(\lambda r.\text{remain-01}(r) \land \text{ARG1}(r,x))$  is generated from the lexeme  $\langle remain, \{remain-01\} \rangle$ and the template  $\lambda v_1 \cdot [S \setminus NP_{[pl]} / (N_{[pl]} / N_{[pl]})$  :  $\lambda f \cdot \lambda x \cdot f(\lambda r \cdot v_1(r) \wedge \operatorname{ARG1}(r, x))]$ . Feature type dimensionality was selected based on the possible number of features for the type. For example, there are many more lexemes than part-of-speech tags, requiring a relatively higher dimensionality for lexeme features. If more than one feature is active for a given feature type, we average the embeddings in the action representation. Additionally, we learn inactive embedding for every feature type, which is used when there are no active features of this type.

## **3** Embedding logical forms

Given a logical form z, its embedded representation is computed by the recursive function  $\psi(z)$ . We use simply-typed lambda calculus logical forms. A logical form is defined with four base cases:

- $\bullet$  Constant c
- Variable v
- Literal  $p(z_1, \ldots, z_k)$ , where the predicate p is a logical form and the arguments  $z_1, \ldots, z_k$  are logical forms
- Lambda term λv.z<sub>1</sub>, where v is a variable and the body z<sub>1</sub> is a logical form

Each logical form is typed. The function  $\psi(z)$  follows these base cases to compute the embedding of z. Algorithm 1 describes  $\psi(z)$ . The recursive combination is achieved with a single-layer neural network parameterized by  $W_r$ ,  $\delta_r$ , and the tanh activation function. The embedding of a constant cis a combination of its name and type embeddings, each derived from a lookup table (line 2). Given a

Algorithm 1  $\psi$ : Embeds a typed lambda calculus expression.

- **Input:** A logical expression or a list of expressions e, embedding lookup tables U and V for logical constants and types.
- **Definitions:** [;] represents concatenation.  $\mathbf{W}_r$  is a  $M_r \times 2M_r$  matrix and  $\delta_r \in \mathbb{R}^{M_r}$  is a bias term. We use c, v, and z for constant, variable, and generic logical form.
- **Output:** Embedding  $\nu \in R^{M_r}$
- 1: CASE *e*:

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2: c: \tanh(\mathbf{W}_r([U[c.name]; V[c.type]]) + \delta_r)
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- 3: v: V[v.type]
- 4:  $p[z_1 \cdots z_k]$ :  $tanh(\mathbf{W}_r[\psi(p); \psi([z_1 \cdots z_k])] + \delta_r)$
- 5:  $[z_1 \cdots z_k]$ : tanh $(\mathbf{W}_r[\psi(z_1); \psi([z_2 \cdots z_k])] + \delta_r)$ 6:  $\lambda v. z$ : tanh $(\mathbf{W}_r[\psi(v); \psi(z)] + \delta_r)$

variable v, its embedding is given via a lookup table V indexed by variable types (line 3). Literals are embedded by recursively embedding their arguments and combining with the predicate embedding (lines 4-5). Finally, for lambda terms, the variable embedding is combined with the body embedding (line 6). The logical form embedding size  $M_r$  is 35. All parameters ( $\mathbf{W}_r, \delta_r$ , and all lookup embeddings) are initialized using the Glorot and Bengio (2010) scheme, similar to the other parameters in the shiftreduce parser.

#### 4 Word Skipping

Since word skipping is never selected during training, the model learns to discourage it. Therefore, we define the term  $\epsilon(a)$ , where  $\epsilon(a) = \gamma$  if the action is a SHIFT that skips the next word, otherwise  $\epsilon(a) = 0$ . In practice, this is accomplished by adding special lexical entries to the lexicon that mark skipping. The probability of action *a* given configuration *c* then incorporates the term  $\epsilon(a)$ :

$$p(a \mid c) = \frac{\exp\left\{\phi(a, c)\mathbf{W}_{b}\mathcal{F}(\xi(c)) + \epsilon(a)\right\}}{\sum_{a' \in \mathcal{A}(c)}\exp\left\{\phi(a', c)\mathbf{W}_{b}\mathcal{F}(\xi(c)) + \epsilon(a')\right\}}$$

We tune  $\gamma$  on a small subset of the development data and set it to  $\gamma = 1.0$ .

#### References

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